

7th semester IMCA Examination- 2019

7.2 Analysis and Design of Algorithm

Full Marks – 70

Time – 3 Hours

Answer All Questions

1	a)	Write the binary search algorithm and its worst case performance analysis.	[4]
	b)	Sort the following elements using merge sort. 23, 78, 12, 43, 21, 80, 62, 48, 66.	[3]
	c)	Solve the following recurrences i) $T(n) = T\left(\frac{n}{2}\right) + 1$ using iteration method ii) $T(n) = T\left(\frac{9n}{10}\right) + n + 8$ using master method	[7]
	d)	iii) Write the recurrence for the time complexity of binary search.	[7]
		OR	
		What is a recurrence relation? Solve the following recurrences using recursion tree method.	
e)	i)	$T(n) = 3T\left(\frac{n}{4}\right) + n$	[3]

	ii) $T(n) = 2T\left(\frac{n}{2}\right) + n$	[4]
f)	Arrange the following functions by the asymptotic order of growth with justifications. $n!, 2^n, \log(n!), n^{\log n}, n^3$ Prove the followings i) $\sum_{i=1}^n i = O(n^2)$ ii) $3n^3 + 5 = w(n)$	
2	Explain the Quick Sort algorithm using divide & conquer approach and find its worst case and best case time complexity. Determine the partitioning position of the given array of elements using Quick sort. $23, 78, 12, 43, 21, 80, 62, 48, 66.$ OR Explain the heap sort algorithm along with the building of heap to sort an array of elements with its time complexity. Sort the given list of elements using heap sort. $18, 23, 78, 12, 43, 21, 80, 62, 48, 66.$	[14]
3	a) What is hashing technique? Explain the different hash functions with the collision resolution techniques. Insert the following elements into a hash table of size 10 with hash function as $H(X)$	[7]

	$= X \text{ mod } \text{table size}$ using linear and quadratic probing. $18, 23, 78, 12, 43, 22, 80, 62, 48, 62.$	
b)	What is 2-3-4 tree? Write the procedure to insert an element into a 2-3-4 tree. Construct a 2-3-4 tree with the given list of elements: $18, 23, 78, 12, 43, 21, 80, 62, 48, 66.$	[7]
c)	OR	[7]
d)	Describe the concept of Amortized Analysis in brief. What is Red Black tree? Construct a red black tree with the following elements. $18, 23, 78, 12, 43, 22, 80, 62, 48, 62.$	[7]
4	a) Determine the shortest path from the given source vertex A to all other vertices in the graph given using Dijkstra's algorithm. <div style="text-align: center;"> <pre> graph LR A((A)) --- 4 B((B)) A --- 7 C((C)) B --- 10 E((E)) B --- 3 D((D)) C --- 8 D C --- 5 F((F)) D --- 5 E D --- 1 F E --- 4 G((G)) F --- 9 G </pre> </div>	[7]
b)	Let $A(3 \times 4)$, $B(4 \times 2)$, $C(2 \times 6)$ and $D(6 \times 3)$ be the chain of matrices to be multiplied.	[7]

	<p>Determine the minimum number of scalar multiplications and the optimal way of parenthesizing the chain of matrices.</p> <p>c) [7]</p> <p style="text-align: center;">OR</p> <p>d) What is MST problem? Write the Prim's algorithm to determine the Minimum Spanning tree and use it in the graph given in Q. 4- (a) to find out the MST. [7]</p> <p>What is greedy choice property? Write the greedy algorithm to solve the fractional knapsack problem. Find an optimal solution to the knapsack instance $n = 7$, $m = 15$, $(p_1, p_2, p_3, p_4, p_5, p_6, p_7) = (10, 5, 15, 7, 6, 18, 3)$, and $(w_1, w_2, w_3, w_4, w_5, w_6, w_7) = (2, 3, 5, 7, 1, 4, 1)$ using greedy technique.</p>
5	<p>a) What is an approximation algorithm? Explain the approximation algorithm to solve vertex cover problem with an example. [7]</p> <p>b) Describe the followings. [7]</p> <p>i) Class P, NP and NP-Complete problems</p> <p>ii) Polynomial reduction</p> <p style="text-align: center;">OR</p> <p>c) Write the implicit and explicit constraints of N-queen problem. Explain the algorithm to solve 4-Queen problem using backtracking approach. [7]</p> <p>d) What is Longest Common Subsequence problem? Let $X = "ABDBADBD"$ and $Y = "BABDAB"$ be the two sequences. Determine the Longest Common Subsequence of X and Y using Dynamic programming approach. [7]</p>

